

PREDICTION OF EXCESS FUNCTIONS OF SOME TERNARY ORGANIC MIXTURES CONTAINING ETHANOL WITH A GROUP CONTRIBUTION MODEL

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ABSTRACT

A study has been made of the performance of the Kehiaian–Guggenheim–Barker group contribution model in the characterization of the excess molar functions of ternary organic mixtures. The present work reports the predictions of the model for the concentration dependence of one set of G^E ternary data and eight sets of H^E ternary data. The nine mixtures, of ethanol, as first component, with *n*-alkanes, cyclohexane and aromatic hydrocarbons, were treated in the framework of the DISQUAC model. The ratios of the standard deviations between experimental and predicted excess molar enthalpies H^E or excess molar Gibbs functions G^E and the maximum values of those excess functions are less than 0.11 for all the systems. Previously obtained parameters for alcohol–aliphatic, alcohol–aromatic and alcohol–cyclic interactions were tested with the binary excess functions H^E , G^E and the excess heat capacity C_p^E , liquid–liquid equilibria and activity coefficients at infinite dilution.

INTRODUCTION

The many empirical equations for the prediction of excess functions can be regarded as different geometrical methods for establishing the contribution to the excess function of each of the three binary mixtures involved [1,2]. Symmetric equations (e.g. Toop's or Coolinet's equations) assign the same weight to each of the three binary contributions, while asymmetric equations (e.g. Hillert's equation) give more weight to the binary contributions 1–2 and 1–3, the role of the component designated as component 1 being very important.

Application of any group contribution model to ternary systems requires much time and effort, but can yield a large quantity of information. Testing the models in areas such as are considered in the present work is therefore very important. We are particularly interested in the behaviour of the DISQUAC model [3,4].

The ternary systems investigated contained four different types of group: aliphatic (CH_3- , $-\text{CH}_2-$), aromatic (C_6H_6 , C_6H_5-), cyclic (C_6H_{12}) and hydroxyl ($-\text{OH}$) groups.

As there are no reports of a system containing an *n*-alcohol having been treated in the framework of the DISQUAC model, it was necessary, as a first step, to obtain parameters corresponding to alcohol–aliphatic, alcohol–aromatic and alcohol–cyclic interactions. Interactions between aliphatic, aromatic and cyclic groups were supposed to be as previously reported [5].

Although the dipolar moments of *n*-alcohols are very similar, regardless of the number of carbon atoms in the *n*-alcohol, their dielectric constants are very different: in dimensionless units and at 298.15 K, 33, 25, 20, 18, 14, 13 and 10, for methanol, ethanol, propanol, butanol, pentanol, hexanol and octanol, respectively. This suggests that it must be necessary, when investigating systems containing an *n*-alcohol, to specify whether this alcohol is methanol, ethanol, or one of higher chain. (We consider this classification to be more suitable than that for the UNIFAC model, where the only distinction made is between methanol and the other alcohols.) For this reason, the present study is limited to systems containing ethanol.

TERNARY SYSTEMS CONSIDERED

Table 1 lists all the ternary systems and binary mixtures considered. Also indicated are the number of data points N , the temperature at which data were taken T , the minimum (F_{\min}^E) and maximum (F_{\max}^E) experimental values (in J mol^{-1}) of the excess functions, and the sources of the data. All data are valid at atmospheric pressure.

ESTIMATION OF INTERACTION PARAMETERS

The theoretical equations of the DISQUAC model may be encountered elsewhere [3,4]. All the geometrical parameters, except those for ethanol, are available from the literature [5]. For ethanol, the volume r is 1.86566, the total surface q 1.7, the fraction of aliphatic surface on an ethanol molecule 0.70385 and that of a hydroxyl 0.29615, all values calculated by Bondi's method. The systems used in the fitting to obtain the interchange parameters are reported in Tables 2–4 (Type a): the H^E and G^E data for ethanol + *n*-hexane of O'Shea and Stokes [12], the G^E data of Hwang and Robinson [30] and H^E data of Stokes and Adamsom [7] for ethanol + cyclohexane, and the G^E data of Smith and Robinson [31] and H^E data of Mrazek and van Ness [10] and van Ness and Abbott [11] for ethanol + benzene.

Experimental G^E and H^E data show that interactions between hydroxyl and aliphatic and cyclic groups are similar. At equimolar composition and 298.15 K, G^E is 1330 for the ethanol + *n*-hexane system and 1395 for ethanol + cyclohexane, and the corresponding H^E values are 580 ($x =$

TABLE 1

Ternary systems and binary mixtures considered in the present work

| No. | System | N | T (K) | F_{\max}^E (J mol ⁻¹) | F_{\min}^E (J mol ⁻¹) | Source of data |
|-----|---|-----|------------|--|--|--|
| 1 | Ethanol + cyclohexane + <i>n</i> -heptane ^a | 11 | 293.15 | 699 | 472 | Grosse-Wortmann et al. (1966) [6] |
| 2 | Ethanol + cyclohexane + <i>n</i> -heptane ^a | 7 | 298.15 | 698 | 595 | Grosse-Wortmann et al. (1966) [6] |
| 3 | Ethanol + cyclohexane + <i>n</i> -heptane ^a | 7 | 303.15 | 796 | 672 | Grosse-Wortmann et al. (1966) [6] |
| 4 | Ethanol + cyclohexane + <i>n</i> -heptane ^a | 7 | 313.15 | 926 | 774 | Grosse-Wortmann et al. (1966) [6] |
| 5 | Ethanol + cyclohexane + <i>n</i> -heptane ^a | 7 | 333.15 | 1375 | 1092 | Grosse-Wortmann et al. (1966) [6] |
| | Ethanol + cyclohexane ^a | | 298.15 | 638 | | Stokes and Adamsom (1977) [7] |
| | Ethanol + <i>n</i> -heptane ^a | | 298.15 | 641 | | Estimated value |
| | <i>n</i> -Heptane + cyclohexane ^a | | 298.15 | 246 | | Grolier (1974) [8] |
| 6 | Ethanol + benzene + <i>n</i> -hexane ^a | 36 | 298.15 | 1173 | 343 | Jones and Lu (1966) [9] |
| | Ethanol + benzene ^a | | 298.15 | 869 | | Mrazek and van Ness (1961) [10] Van Ness and Abbott (1976) [11] |
| | Ethanol + <i>n</i> -hexane ^a | | 298.15 | 580 | | O'Shea and Stokes (1986) [12] |
| | <i>n</i> -Hexane + benzene ^a | | 298.15 | 897 | | Paz Andrade (1973) [13] |
| 7 | Ethanol + benzene + <i>n</i> heptane ^a | 26 | 298.15 | 1227 | 232 | Lu and Jones (1966) [14] |
| | <i>n</i> -Heptane + benzene ^a | | 298.15 | 937 | | Müncksch (1978) [15] |
| 8 | Ethanol + cyclohexane + toluene ^a | 18 | 298.15 | 1106 | 223 | Schainable et al. (1957) [16] |
| | Ethanol + toluene ^a | | 298.15 | 820 | | Mrazek and van Ness (1961) [10] Van Ness and Abbott (1976) [11] |
| | Cyclohexane + toluene ^a | | 298.15 | 628 | | Hsu and Clever (1975) [17] |
| 9 | <i>n</i> -Hexane + ethanol + benzene ^b | 35 | 328.15 | 1536 | 576 | Yuan et al. (1963) [18] |
| | Ethanol + <i>n</i> -hexane ^b | | 328.15 | 1414 | | Yuan et al. (1963) [18] |
| | Ethanol + benzene ^b | | 328.15 | 1130 | | Yuan et al. (1963) [18] |
| | <i>n</i> -Hexane + benzene ^b | | 328.15 | 358 | | Yuan et al. (1963) [18] |

^a Excess function: H^E .^b Excess function: G^E .

TABLE 2

Molar excess enthalpies H^E and molar excess Gibbs energies G^E for ethanol + n -alkane mixtures at various temperatures T and compositions x_1 at which the excess function is maximum: Comparison of direct experimental results with values calculated using coefficients from Table 5

| n -Alkane | Data | T (K) | x_1 | Exp. (J mol ⁻¹) | Calc. (J mol ⁻¹) | Source of data |
|----------------------|-------|---------------------|--------|-----------------------------|------------------------------|---------------------------------|
| n -C ₆ | G^E | 283.15 ^a | 0.5 | 1330 | 1337 | O'Shea and Stokes (1986) [12] |
| | | 298.15 ^a | 0.5 | 1374 | 1381 | O'Shea and Stokes (1986) [12] |
| | | 313.15 | 0.5 | 1424 | 1418 | Janaszewski et al., (1982) [19] |
| | | 318.15 ^a | 0.4684 | 1425 | 1431 | O'Shea and Stokes (1986) [12] |
| n -C ₇ | G^E | 303.15 | 0.5 | 1454 | 1436 | Van Ness and Abbott (1977) [20] |
| | | 313.15 | 0.5 | 1463 | 1459 | Janaszewski et al. (1982) [19] |
| | | 323.15 | 0.5 | 1482 | 1476 | Van Ness and Abbott (1977) [20] |
| | | 343.17 | 0.5288 | 1498 | 1484 | Berro et al. (1982) [21] |
| n -C ₈ | G^E | 313.15 | 0.5 | 1494 | 1488 | Janaszewski et al. (1982) [19] |
| n -C ₉ | G^E | 343.21 | 0.5076 | 1559 | 1531 | Berro et al. (1982) [21] |
| n -C ₅ | H^E | 298.15 | 0.4282 | 534 | 535 | Collins et al. (1980) [22] |
| n -C ₆ | H^E | 283.15 ^a | 0.3871 | 441 | 453 | O'Shea and Stokes (1986) [12] |
| | | 298.15 ^a | 0.3669 | 580 | 592 | O'Shea and Stokes (1986) [12] |
| | | 318.15 ^a | 0.3398 | 855 | 879 | O'Shea and Stokes (1986) [12] |
| n -C ₇ | H^E | 303.15 | 0.4145 | 666 | 705 | Shatas et al. (1975) [23] |
| | | 323.15 | 0.3741 | 986 | 1060 | Shatas et al. (1975) [23] |
| n -C ₈ | H^E | 293.15 | 0.4589 | 587 | 622 | Ragaini et al. (1968) [24] |
| | | 298.15 | 0.4699 | 644 | 679 | Ragaini et al. (1968) [24] |
| | | 308.15 | 0.4388 | 708 | 831 | Ragaini et al. (1968) [24] |
| | | 298.15 | 0.3829 | 700 | 730 | Christensen et al. (1979) [25] |
| n -C ₉ | H^E | 303.15 | 0.5 | 730 | 875 | Savini et al. (1965) [26] |
| | | 318.15 | 0.5 | 955 | 1053 | Savini et al. (1965) [26] |
| | | 298.15 | 0.379 | 713 | 809 | Pfestorf et al. (1983) [27] |
| n -C ₁₁ | H^E | 308.15 | 0.37 | 911 | 993 | Pfestorf et al. (1983) [27] |
| | | 308.15 | 0.4327 | 948 | 1134 | Ramalho and Ruel (1969) [28] |
| n -C ₁₄ | H^E | 313.15 | 0.4184 | 1048 | 1260 | Ramalho and Ruel (1969) [28] |
| | | 325.25 | 0.3752 | 1461 | 1735 | French et al. (1979) [29] |

^a System used in the determination of interchange energy coefficients of alcohol-aliphatic interaction.

0.3669) and 638 ($x_1 = 0.4194$), all values being given in J mol⁻¹. We may therefore suppose that the differences between these kinds of systems are due mainly to dispersive forces, i.e. the differences will be associated with different dispersive coefficients, as is also the case in binary mixtures containing chloroalkanes and n -alkanes or cyclohexane [32]. On the other hand, if c_i , c_i^* are determined separately, the following values are obtained: $c_1^* = 1.775$, $c_2^* = 0.526$, $c_3^* = -10.12$, $c_1 = 12.41$, $c_2 = 13.60$, $c_3 = 70.87$ for the hydroxyl-aliphatic interaction; and $c_1^* = 2.156$; $c_2^* = 0.7286$, $c_3^* = -9.864$, $c_1 = 11.86$, $c_2 = 11.07$, $c_3 = 71.28$ for the cyclic-hydroxyl interaction. Here we can see that the quasi-chemical coefficients are very similar.

TABLE 3

Molar excess enthalpies H^E and molar excess Gibbs energies G^E for ethanol+cyclohexane mixtures at various temperatures T and compositions x_1 at which the excess function is maximum: Comparison of direct experimental results with values calculated using coefficients from Table 5

| Data ^a | T (K) | x_1 | Exp. (J mol ⁻¹) | Calc. (J mol ⁻¹) | Source of data |
|-------------------|------------|--------|--------------------------------|---------------------------------|--------------------------------|
| G^E | 298.15 | 0.5 | 1387 | 1397 | Hwang and Robinson (1977) [30] |
| H^E | 283.15 | 0.4721 | 533 | 552 | Stokes and Adamsom (1977) [7] |
| | 288.15 | 0.4661 | 562 | 581 | Stokes and Adamsom (1977) [7] |
| | 293.15 | 0.42 | 593 | 617 | Stokes and Adamsom (1977) [7] |
| | 298.15 | 0.4194 | 638 | 658 | Stokes and Adamsom (1977) [7] |
| | 308.15 | 0.4202 | 738 | 759 | Stokes and Adamsom (1977) [7] |
| | 318.15 | 0.3824 | 870 | 892 | Stokes and Adamsom (1977) [7] |

^a All systems used in determination of interchange energy coefficients of alcohol-cyclic interaction.

As a result, to reduce the set of parameters we chose as common parameters $c_1 = 12.2$, $c_2 = 12.2$, $c_3 = 71.1$. The dispersive coefficients were calculated separately. Final results are given in Table 5.

TABLE 4

Molar excess enthalpies H^E and molar excess Gibbs energies G^E for ethanol+benzene or toluene mixtures at various temperatures T and equimolar composition or $x_1 = 0.3$ (where H^E is maximum): Comparison of direct experimental results with values calculated using coefficients from Table 5

| Component 2 | Data | T (K) | x_1 | Exp. (J mol ⁻¹) | Calc. (J mol ⁻¹) | Source of data |
|-------------|--------------------|------------|-------|--------------------------------|---------------------------------|---------------------------------|
| Benzene | G^E ^a | 298.15 | 0.5 | 1076 | 1070 | Smith and Robinson (1970) [31] |
| Toluene | G^E | 303.15 | 0.5 | 1179 | 1112 | Van Ness and Abbott (1977) [20] |
| | G^E | 333.15 | 0.5 | 1203 | 1127 | Van Ness and Abbott (1977) [20] |
| Benzene | H^E ^a | 298.15 | 0.3 | 869 | 875 | Mrazek and van Ness (1961) [10] |
| | | | 0.5 | 761 | 750 | Van Ness and Abbott (1976) [11] |
| | H^E ^a | 308.15 | 0.3 | 1020 | 1027 | Van Ness and Abbott (1976) [11] |
| | | | 0.5 | 909 | 897 | Van Ness and Abbott (1976) [11] |
| Toluene | H^E ^a | 318.15 | 0.3 | 1154 | 1190 | Van Ness and Abbott (1976) [11] |
| | | | 0.5 | 1079 | 1057 | Van Ness and Abbott (1976) [11] |
| | H^E | 298.15 | 0.3 | 820 | 776 | Van Ness and Abbott (1976) [11] |
| | | | 0.5 | 721 | 644 | Van Ness and Abbott (1976) [11] |
| | H^E | 308.15 | 0.3 | 986 | 935 | Van Ness and Abbott (1976) [11] |
| | | | 0.5 | 880 | 794 | Van Ness and Abbott (1976) [11] |
| H^E | 318.15 | 0.3 | 1157 | 1109 | Van Ness and Abbott (1976) [11] | |
| | | | 0.5 | 1043 | 964 | Van Ness and Abbott (1976) [11] |

^a Systems used in the determination of interchange energy coefficients of alcohol-aromatic interaction.

TABLE 5

Interchange energy coefficients, dispersive c_i^* and quasichemical c_i , used in the present work, for an alcohol group in ethanol

| Interaction | c_1^* | c_2^* | c_3^* | c_1 | c_2 | c_3 | Source of data |
|--------------------|---------|---------|---------|-------|-------|-------|----------------------------|
| Alcohol-aliphatic | 1.84 | 0.81 | -9.07 | 12.2 | 12.2 | 71.1 | Present work |
| Alcohol-cyclic | 2.15 | 0.88 | -9.05 | 12.2 | 12.2 | 71.1 | Present work |
| Alcohol-aromatic | 1.67 | -2.54 | -11.2 | 8.934 | 16.7 | 21.21 | Present work |
| Aliphatic-cyclic | 0.05123 | 0.1533 | 0 | 0 | 0 | 0 | Kehiaian et al. (1978) [5] |
| Aliphatic-aromatic | 0.2598 | 0.5623 | 0 | 0 | 0 | 0 | Kehiaian et al. (1978) [5] |
| Cyclic-aromatic | 0.2455 | 0.5619 | 0 | 0 | 0 | 0 | Kehiaian et al. (1978) [5] |

A test to show whether our argument was correct was carried out as follows. Consider the ethanol + cyclohexane system. From the H^E and G^E experimental data we subtracted the contribution due to hydroxyl-aliphatic

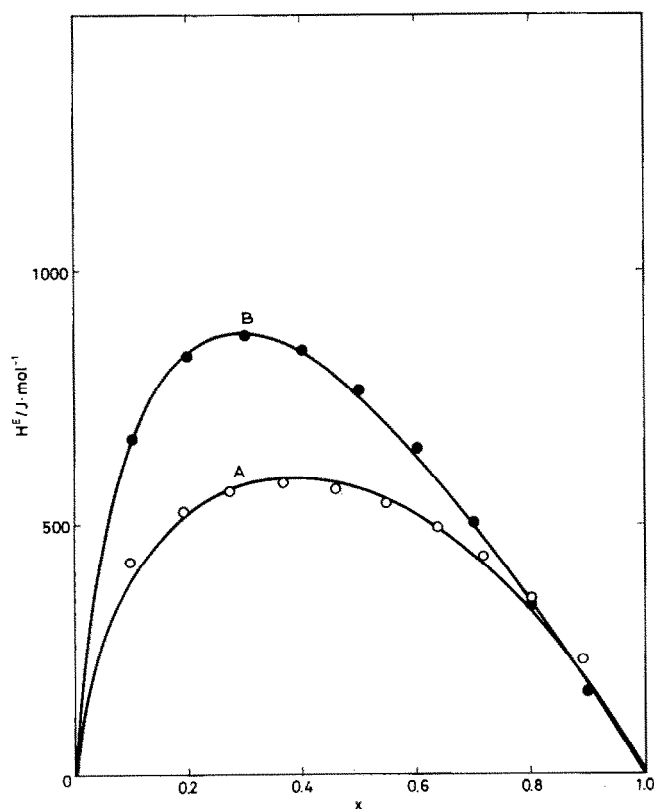


Fig. 1. Comparison of theoretical with experimental values of molar excess enthalpy H^E at 298.15 K for the mixtures ethanol(1) + *n*-hexane(2) (curve A) and ethanol(1) + benzene(2) (curve B) vs. x_1 . Solid lines, predicted values; symbols, experimental values: \circ *n*-hexane (O'Shea and Stokes [12]), \bullet benzene (van Ness and Abbott [11]).

interaction calculated with our final parameters. The dispersive coefficients relating to the aliphatic-cyclic interaction were then calculated, and the values obtained ($c_1^* = 0.075$, $c_2^* = 0.1633$) were very similar to those reported in ref. 5. Naturally, to obtain a correct value for c_1^* it is necessary to take into account the size effect related to the combinatorial term of G^E (at equimolar composition and 298.15 K, $G_{\text{comb}}^E = -5 \text{ J mol}^{-1}$ for *n*-hexane + cyclohexane and -123 J mol^{-1} for ethanol + cyclohexane). Unfortunately, it is not possible to proceed in a similar fashion for systems containing benzene, owing to the more polarizable nature of this molecule. This is very clear from the H^E values for the *n*-hexane + cyclohexane and benzene + *n*-hexane systems: 200 and 900 J mol⁻¹, respectively, at equimolar composition and 298.15 K.

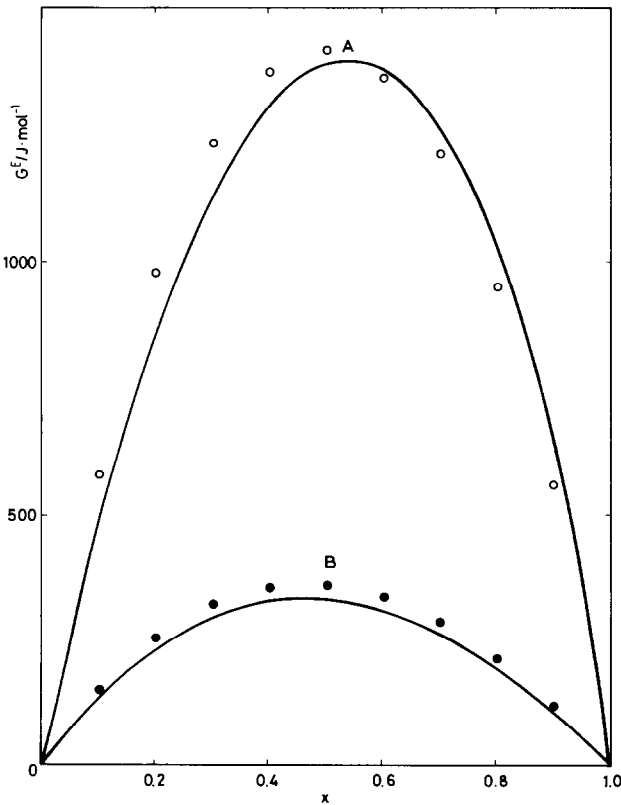


Fig. 2. Comparison of theoretical with experimental values of molar excess Gibbs energy G^E at 328.15 K for the mixtures *n*-hexane(1) + ethanol(2) (curve A) and *n*-hexane(1) + benzene(2) (curve B) vs. x_1 . Solid lines, predicted values; symbols, values obtained using eqn. (6) from Yuan et al. [18]: \circ ethanol, \bullet benzene.

RESULTS AND DISCUSSION

Comparison of the experimental values of H^E and G^E and those predicted by the DISQUAC model (Tables 2–4) shows fairly good agreement between them. The greatest differences encountered are for ethanol + *n*-alkane systems when the *n*-alkane is one of long chain (*n*-tetradecane or *n*-hexadecane). For this reason, critical temperatures calculated for systems such as ethanol + *n*-tetradecane (55 °C) or ethanol + *n*-hexadecane (67.75 °C) are higher than the experimental values (35 [28] and 52.2 °C [29], respectively). The predicted critical compositions are more suitable: 0.797

TABLE 6

Logarithms of activity coefficients at infinite dilution $\ln \gamma_i^\infty$ in mixtures containing ethanol and *n*-alkane (*n*-hexane, *n*-heptane) or benzene or toluene: Comparison of experimental results with values calculated using coefficients from Table 5

| Component 2 | <i>T</i> (K) | $\ln \gamma_1^\infty$ | | $\ln \gamma_2^\infty$ | | Source of data |
|----------------------|-----------------|-----------------------|-------|-----------------------|-------|---------------------------------|
| | | Exp. | Calc. | Exp. | Calc. | |
| <i>n</i> -Hexane | 283.15 | 4.514 | 4.534 | 2.42 | 2.00 | O'Shea and Stokes (1986) [12] |
| | 298.15 | 4.02 | 4.27 | 2.37 | 2.30 | O'Shea and Stokes (1986) [12] |
| | 318.15 | 3.44 | 3.88 | 2.29 | 2.12 | O'Shea and Stokes (1986) [12] |
| <i>n</i> -Heptane | 303.15 | 4.72 | 4.09 | 2.65 | 2.47 | Ronc and Ratcliff (1976) [33] |
| | | 4.05 | | 2.60 | | Van Ness and Abbott (1977) [20] |
| | 323.15 | 3.43 | 3.64 | 2.45 | 2.41 | Van Ness and Abbott (1977) [20] |
| Benzene ^a | 298.15 | 2.53 | 3.00 | 1.502 | 1.54 | Smith and Robinson (1970) [31] |
| Toluene | 303.15 | 2.95 | 2.99 | 1.87 | 1.66 | Van Ness and Abbott (1977) [20] |
| | 318.15 | 2.53 | 2.66 | 1.72 | 1.62 | Van Ness et al. (1967) [34] |
| | 333.15 | 2.30 | 2.35 | 1.62 | 1.58 | Van Ness et al. (1967) [34] |

^a Values estimated from Redlich–Kister equation with four coefficients.

TABLE 7

Comparison of direct experimental results with values obtained in the present work using coefficients from Table 5

| System | F_{\max}^E (J mol ⁻¹) | | F_{\min}^E (J mol ⁻¹) | | σ |
|--------|-------------------------------------|-------|-------------------------------------|-------|----------|
| | Exp. | Calc. | Exp. | Calc. | |
| 1 | 699 | 733 | 472 | 460 | 22 |
| 2 | 698 | 779 | 595 | 645 | 75 |
| 3 | 796 | 844 | 672 | 687 | 41 |
| 4 | 926 | 985 | 774 | 792 | 55 |
| 5 | 1375 | 1381 | 1092 | 1101 | 89 |
| 6 | 1173 | 1304 | 343 | 391 | 12 |
| 7 | 1227 | 1386 | 232 | 200 | 103 |
| 8 | 1106 | 1023 | 223 | 167 | 99 |
| 9 | 1536 | 1399 | 576 | 527 | 80 |

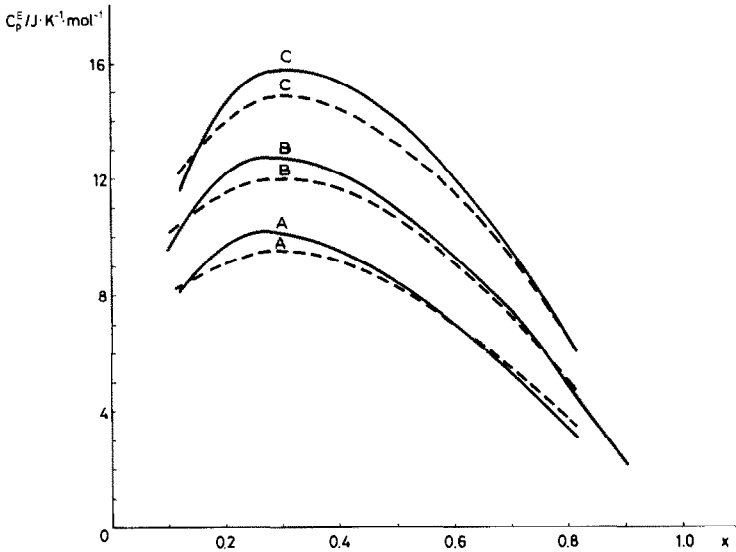


Fig. 3. Comparison of theoretical with experimental values of molar excess heat capacity C_p^E vs. x_1 at temperatures 288.15 K (curves A), 298.15 K (curves B) and 308.15 K (curves C) for the mixture ethanol(1) + *n*-heptane(2). Solid lines, predicted values; dashed lines, experimental results from Brown and Ziegler [35].

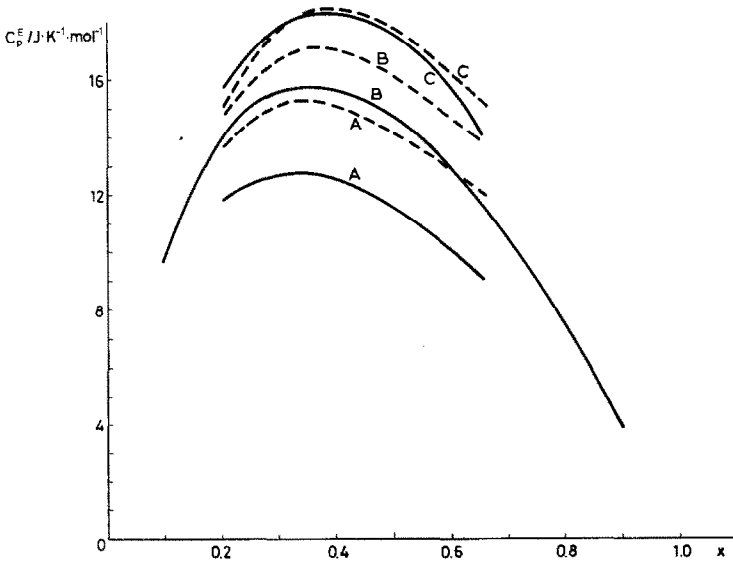


Fig. 4. Comparison of theoretical with experimental values of molar excess heat capacity C_p^E vs. x_1 at temperatures 288.15 K (curves A), 303.15 K (curves B) and 318.15 K (curves C) for the mixture ethanol(1) + toluene(2). Solid lines, predicted values; dashed lines, experimental results from Brown and Ziegler [35].

for the former mixture (experimental value, 0.77) and 0.817 for the latter (experimental value, 0.8197).

The shapes of the excess curves, i.e. H^E , G^E dependence on concentration, are also correct (see Figs. 1 and 2). With the coordination number used ($z = 4$), we obtain H^E curves shifted towards the low concentration region in ethanol, and fairly symmetrical G^E curves. Again, the curves for the higher n -alkanes are slightly less symmetrical, as a result of differences between experimental and calculated critical compositions in systems with miscibility gaps.

Table 6 lists values of $\ln \gamma_i^\infty$, with differences $\Delta \ln \gamma_i^\infty = \ln \gamma_i^\infty$ (experimental) $- \ln \gamma_i^\infty$ (predicted) being negative when $i = 1$ and positive when $i = 2$. (The ethanol + benzene system must not be considered, as the $\ln \gamma_i^\infty$ values were obtained not experimentally, but rather from a Redlich–Kister equation with four coefficients.)

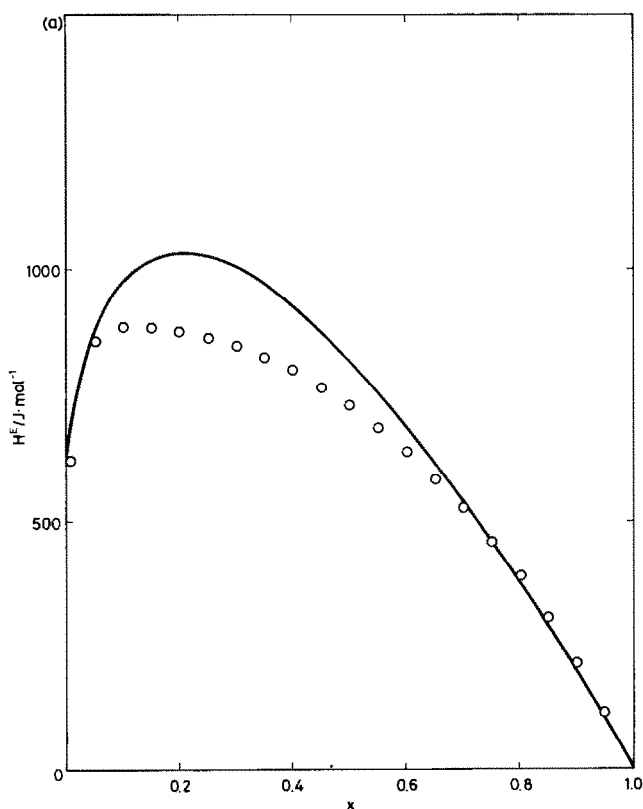


Fig. 5a. Comparison of theoretical with experimental values of molar excess enthalpy H^E for the mixture ethanol(1)+benzene(2)+ n -hexane(3) vs. x_1 at 298.15 K and $x_2/x_3 = 0.3333$. Solid lines, predicted values; \circ , values obtained using a van Ness correlation equation with ten coefficients fitted using ternary data from Jones and Lu [9].

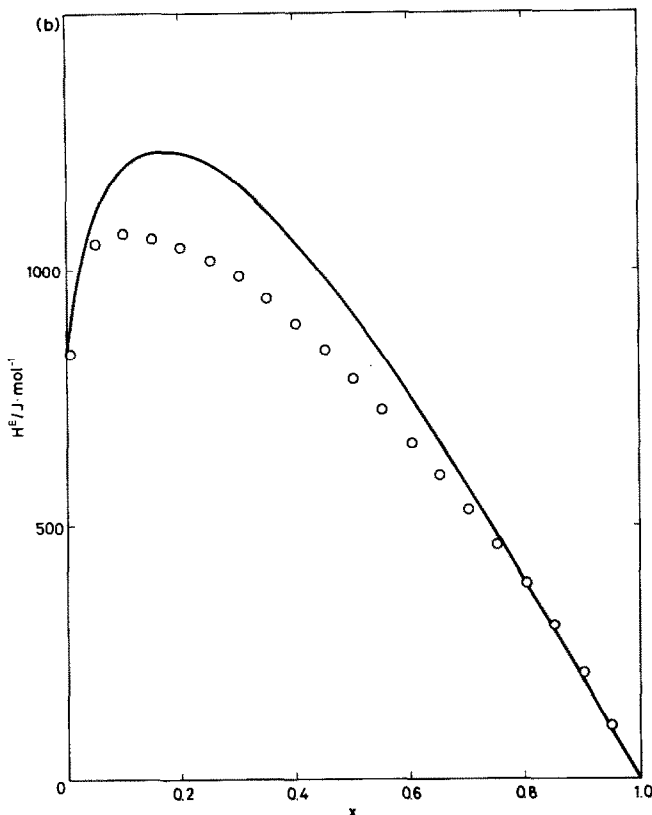


Fig. 5b. Comparison of theoretical with experimental values of molar excess enthalpy H^E for the mixture ethanol(1)+benzene(2)+*n*-hexane(3) vs. x_1 at 298.15 K and $x_2/x_3 = 0.6666$. Solid lines, predicted values; \circ , values obtained using a van Ness correlation equation with ten coefficients fitted using ternary data from Jones and Lu [9].

In the case of the ethanol + toluene mixtures, the curves of G^E (experimental) vs. x_1 are shifted slightly to the right in comparison with the curves predicted by the DISQUAC model. In the case of the ethanol + *n*-alkane systems, we think the $\Delta \ln \gamma_i^\infty$ values are related to the Flory-Huggins equation, which is known to overestimate the combinatorial entropy. In effect, while there is good agreement between the shapes and sizes of the TS^E vs. x_1 curves for the ethanol + benzene system (at 298.15 K), the same is not the case for the ethanol + *n*-hexane system (at the same temperature). The DISQUAC model predicts a change in sign (at the same temperature, and with $x = 0.01$) of the excess entropy, with $TS^E \approx 2 \text{ J mol}^{-1}$, but experimentally, although TS^E does change in sign at a similar concentration, its value is greater (44 J mol^{-1}).

It is very important that the DISQUAC model gives fairly good predictions of the variation of C_p^E with temperature and concentration [35,36,37] (see Figs. 3 and 4). C_p^E always increases with temperature in the case of the

ethanol + *n*-heptane mixture, but decreases, from a certain temperature, in the case of the ethanol + toluene system. We think this is a success of the DISQUAC model, and a justification of our parameters, particularly of the third interchange coefficients.

The results of our comparison of experimental and predicted values, maximum and minimum, (all in J mol^{-1}) for the ternary systems considered are given in Table 7. The standard deviations σ , defined as

$$\sigma = \left[\frac{(F_{\text{calc}}^E - F_{\text{exp}}^E)^2}{N} \right]^{1/2} \quad (1)$$

are also listed. Table 1 lists the binary mixtures involved in these ternary systems. These have greater excess functions than the former. In the ternary mixtures containing only *n*-alkane, aromatic or cyclic compounds, this is not the case, owing to the presence of dispersive forces only. In the present case,

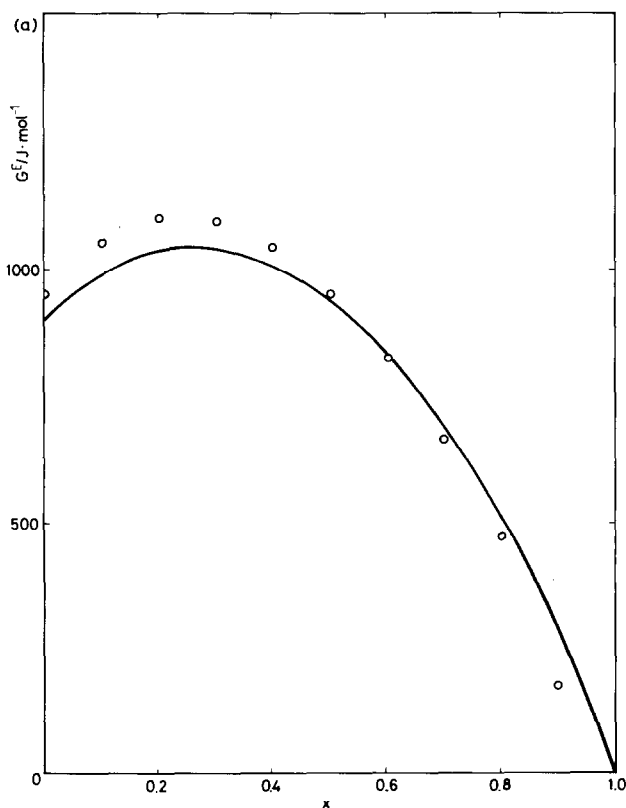


Fig. 6a. Comparison of theoretical with experimental values of molar excess Gibbs energy G^E for the mixture *n*-hexane(1) + ethanol(2) + benzene(3) vs. x_1 at 328.15 K and $x_2/x_3 = 0.3333$. Solid lines, predicted values; \circ , values obtained using eqn. (6) from Yuan et al. [18].

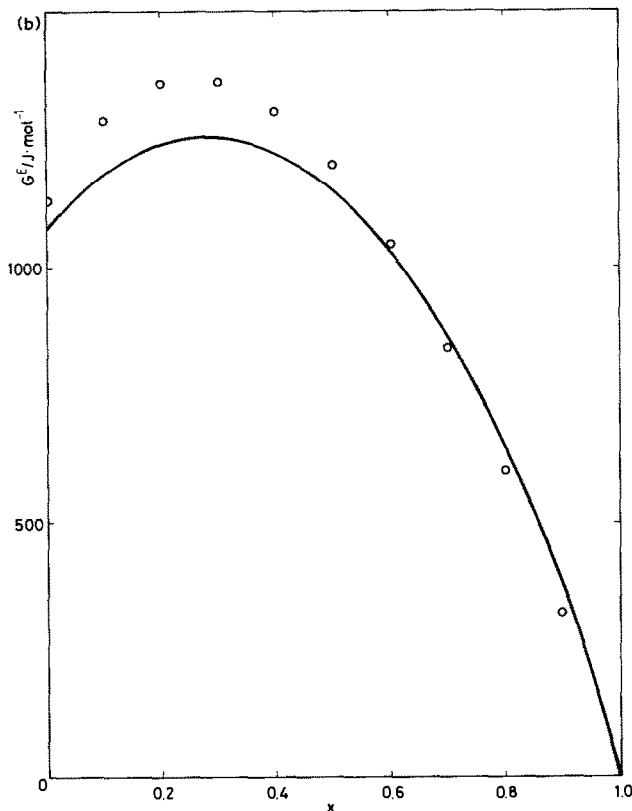


Fig. 6b. Comparison of theoretical with experimental values of molar excess Gibbs energy G^E for the mixture *n*-hexane(1) + ethanol(2) + benzene(3) vs. x_1 at 328.15 K and $x_2/x_3 = 0.6666$. Solid lines, predicted values; \circ , values obtained using eqn. (6) from Yuan et al. [18].

with an alcohol in the mixture, each component makes a different contribution to the breaking of the hydrogen bond.

Values for the ternary mixtures ethanol + benzene + *n*-hexane (H^E at 298.15 K) and *n*-hexane + ethanol + benzene (G^E at 328.15 K) are plotted in Figs. 5 and 6, respectively, for two different concentration ratios, $x_2/x_3 = 0.3333$ and 0.6666. We can see that predictions are good for these ternary systems.

The calculated values are greater than the experimental data, except in two cases. In the ethanol + cyclohexane + toluene mixture, with six different interactions, this is related to the H^E prediction for the ethanol + toluene system. Table 4 shows that the theoretical values are smaller than the experimental ones, which means that the interchange coefficients do not compensate sufficiently for the decrease of aromatic surface. Thus, at the maximum for this ternary system, the dispersive contribution of the alcohol–aromatic interaction is about -260 J mol^{-1} , which is too negative when compared with the other contributions (see Table 8).

TABLE 8

Contributions to H^E of different interactions in the ethanol + cyclohexane + toluene system

| Interaction | Dispersive (J mol ⁻¹) | | Quasi-chemical (J mol ⁻¹) | | Total (J mol ⁻¹) | |
|--------------------|--------------------------------------|------|--|------|---------------------------------|------|
| | Max. | Min. | Max. | Min. | Max. | Min. |
| Alcohol-aliphatic | -89 | -67 | -53 | -63 | -142 | -130 |
| Alcohol-cyclic | 64 | 47 | 171 | 68 | 235 | 115 |
| Alcohol-aromatic | -260 | -197 | 760 | 291 | 500 | 94 |
| Aliphatic-cyclic | 68 | 20 | 0 | 0 | 68 | 20 |
| Aliphatic-aromatic | -30 | 59 | 0 | 0 | -30 | 59 |
| Cyclic-aromatic | 391 | 8 | 0 | 0 | 391 | 8 |

In the case of the ethanol + benzene + *n*-hexane system, the differences [$G^E(\text{calculated}) - G^E(\text{experimental})$] are negative, while the corresponding H^E differences are positive. This may be due to the special form of the $\ln \gamma_i$ expression. The ethanol + benzene mixture has the same number of groups as the actual ternary system; but in this ternary system the presence of *n*-hexane results in an extra negative term ($zq_i \ln(X_{\text{aliphatic}}/\alpha_{\text{aliphatic}})$). Only when the *n*-hexane concentration is high (0.7, 0.8) do the G^E differences become positive, owing to the greater weight of the dispersive contribution to G^E . Naturally, this behaviour needs to be studied in systems where the third component has more than one group.

REFERENCES

- 1 C. Pando, J.A.R. Renuncio, J.A.G. Calzon, J.J. Christensen and R.M., Izatt, J. Solution Chem., 16 (1987) 503.
- 2 W.E. Acree, Jr., Thermodynamic Properties of Non-Electrolyte Solutions, Academic Press, London, 1984, Chap. 4.
- 3 K.V. Kehiaian and B. Marongiu, Fluid Phase Equilibria, 21 (1985) 197.
- 4 J. Muñoz Embid, O. Santos, I. Velasco, C. Gutiérrez Losa and H.V. Kehiaian, Fluid Phase Equilibria, 38 (1987) 1.
- 5 H.V. Kehiaian, J.-P. Grolier and G.C. Benson, J. Chim. Phys., 75 (1978) 1031.
- 6 H. Grosse-Wortmann, W. Jost and H.G. Wagner, Z. Phys. Chem., 70 (1966) 602.
- 7 R.H. Stokes and M. Adamsom, J. Chem. Soc., Faraday Trans. 1, (1977) 1232.
- 8 J.P. Grolier, Int. Data Ser. Sel. Data Mixtures, Ser. A, N3 (1974) 217.
- 9 H.K.DeQ. Jones and B.C.-Y. Lu, J. Chem. Eng. Data, 11 (1966) 488.
- 10 P.V. Mrazek and H.C. van Ness, AIChE J., 7 (1961) 190.
- 11 H.C. van Ness and M.M. Abbott, Int. Data Ser. Sel. Data Mixtures, Ser. A, N1 (1976) 20, 28.
- 12 S.J. O'Shea and R.H. Stokes, J. Chem. Thermodyn., 18 (1986) 691.
- 13 M.I. Paz Andrade, Int. Data Ser. Sel. Data Mixtures, Ser. A, N2 (1973) 96.
- 14 B.C.-Y. Lu and H.K.DeQ. Jones, Can. J. Chem. Eng., 44 (1966) 251.
- 15 E. Müncsch, Thermochem. Acta, 22 (1978) 237.
- 16 H.W. Schainable, H.C. van Ness and J.M. Smith, AIChE J., 3 (1957) 147.

- 17 K.-Y. Hsu and H.L. Clever, *J. Chem. Thermodyn.*, 7 (1975) 435.
- 18 K.S. Yuan, J.C.K. Ho, A.K. Keshpande and B.C.-Y. Lu, *J. Chem. Eng. Data*, 8 (1963) 549.
- 19 B. Janaszewski, P. Oracz, M. Goral and S. Warycha, *Fluid Phase Equilibria*, 9 (1982) 295.
- 20 H.C. van Ness and M.M. Abbott, *Int. Data Ser. Sel. Data Mixtures, Ser. A*, 1 (1977) 1.
- 21 C. Berro, M. Rogalski and A. Peneloux, *Fluid Phase Equilibria*, 8 (1982) 55.
- 22 S.G. Collins, J.J. Christensen, R.M. Izatt and R.W. Hanks, *J. Chem. Thermodyn.*, 12 (1980) 609.
- 23 J.P. Shatas, M.M. Abbott and H.C. van Ness, *J. Chem. Eng. Data*, 20 (1975) 406.
- 24 V. Ragaini, R. Santi and S. Carra, *Lincei-Rend. Sci. Fis. Mat. e Nat.*, 45 (1968) 540.
- 25 J.J. Christensen, R.M. Izatt, B.D. Stitt, R.W. Hanks and K.D. Williamson, *J. Chem. Thermodyn.*, 11 (1979) 1029.
- 26 C.G. Savini, D.R. Winterhalter and H.C. van Ness, *J. Chem. Eng. Data*, 10 (1965) 168.
- 27 R. Pfestorf, J. Schumelzer, M. Krug, B. Zeiger, U. Stych, and K. Quitzsch, *Fluid Phase Equilibria*, 12 (1983) 283.
- 28 R.S. Ramalho and M. Ruel, *J. Chem. Eng. Data*, 14 (1969) 20.
- 29 H.T. French, A. Richards and R.H. Stokes, *J. Chem. Thermodyn.*, 11 (1979) 671.
- 30 S.C. Hwang and R.L. Robinson, *J. Chem. Eng. Data*, 22 (1977) 319.
- 31 V.C. Smith and R.L. Robinson, *J. Chem. Eng. Data*, 15 (1970) 391.
- 32 H.V. Kehiaian and B. Marongiu, *Fluid Phase Equilibria*, 40 (1988) 23.
- 33 M. Ronc and C.R. Ratcliff, *Can. J. Chem. Eng.*, 54 (1976) 326.
- 34 H.C. van Ness, C.A. Socek, G.L. Peloquin and R.L. Machado, *J. Chem. Eng. Data*, 12 (1967) 217.
- 35 N.G. Brown, Jr. and W.T. Ziegler, *J. Chem. Eng. Data*, 24 (1979) 319.
- 36 M.J. Pedersen, W.B. Kay and H. Hershey, *J. Chem. Thermodyn.*, 7 (1975) 1107.
- 37 S.C.P. Hwa and W.T. Ziegler, *J. Phys. Chem.*, 70 (1966) 2572.